

DIVISIBILITY CRITERIA

A number is divisible by:

2 if the number is even or ends in zero

3 if the sum of the digits is divisible by 3

4 if the last two digits are divisible by 4

Ex: 2316 is divisible by 4 because 16 is divisible by 4

5 if the last digit is 5 or zero

6 if the last digit is even and the sum of the digits is divisible by 3

7 if you delete the units digit, subtract twice the units digit from the remaining number, and the answer is divisible by 7

Ex:
$$\begin{array}{r} 16\cancel{9} \\ -2 \\ \hline 14 \end{array}$$
 is divisible by 7

8 if the last three digits are divisible by 8

Ex: 1168 is divisible by 8 because 168 is divisible by 8

9 if the sum of digits is divisible by 9

11 if the difference between the sum of the digits in even places and the sum of the digits in odd places is equal to zero or 11

Ex: for 649, $(6 + 9) - 4 = 11$, so 649 is divisible by 11

or: if you delete the units digit, subtract the units digit from the remaining number, and the answer is divisible by 11

Ex:
$$\begin{array}{r} 64\cancel{9} \\ -9 \\ \hline 55 \end{array}$$
 is divisible by 11

- 13 if you delete the units digit, add 4 times the units digit to the remaining number, and the answer is divisible by 13

$$\text{Ex: } \begin{array}{r} 19\cancel{7} \\ +20 \\ \hline 39 \end{array} \text{ is divisible by 13}$$

- 17 if you delete the units digit, subtract 5 times the units digit from the remaining number, and the answer is divisible by 17

$$\text{Ex: } \begin{array}{r} 39\cancel{7} \\ -5 \\ \hline 34 \end{array} \text{ is divisible by 17}$$

- 19 if you delete the units digit, add twice the units digit to the remaining number, and the answer is divisible by 19

$$\text{Ex: } \begin{array}{r} 43\cancel{7} \\ +14 \\ \hline 57 \end{array} \text{ is divisible by 19}$$

Note: the tests can be performed multiple times in succession.

In the last example: $\begin{array}{r} 43\cancel{7} \\ +14 \\ \hline 57 \end{array} \rightarrow \begin{array}{r} 5\cancel{7} \\ +14 \\ \hline 19 \end{array} \text{ is divisible by 19}$